

What do I need to be able to do?

- Use equivalence to simplify, compare and order fractions
- Four operations with fractions
- Four operations with mixed numbers
- Fractions of amounts, including finding the original amount
- Solve problems with fractions on a calculator
- 'Show that' questions

Add and subtract algebraic fractions

Multiply and divide algebraic fractions

Keywords:

Numerator : the number above the line on a fraction. The top number.

Denominator: the number below the line on a fraction. The bottom number

Improper Fraction: numerator is larger than the denominator

Mixed Number: a whole number with a fraction eg $2\frac{1}{5}$

Reciprocal: the result of dividing 1 by that number. Flip a fraction to get its reciprocal

ORDERING FRACTIONS

Use equivalent fractions with the same denominator.

Put these fractions in order, from smallest to largest.

$$\begin{array}{ccc} \frac{3}{5} & \frac{1}{2} & \frac{3}{4} \\ \downarrow & \downarrow & \downarrow \\ \frac{12}{20} & \frac{10}{20} & \frac{15}{20} \end{array}$$

Rewrite the original fractions in size order.

$$\frac{1}{2} \quad \frac{3}{5} \quad \frac{3}{4}$$

ADDING/SUBTRACTING FRACTIONS

When we add or subtract fractions we must have a common denominator.

$$\frac{1}{6} + \frac{5}{9} = \frac{3}{18} + \frac{10}{18} = \frac{13}{18}$$

Numerator & Denominator $\times 3$ Numerator & Denominator $\times 2$

MULTIPLYING FRACTIONS

To quickly multiply fractions we multiply the numerators and multiply the denominators

$$\frac{5}{6} \times \frac{3}{5} = \frac{15}{30} = \frac{1}{2}$$

(5 x 3) = (15) Can we simplify this fraction?

(6 x 5) = (30)

DIVIDING FRACTIONS

Dividing is the same as multiplying by the reciprocal.

$$\frac{2}{3} \div \frac{1}{5} = \frac{2}{3} \times \frac{5}{1} = \frac{10}{3} = 3\frac{1}{3}$$

Change the sign. Flip the divisor. KEEP CHANGE FLIP

CALCULATING WITH MIXED NUMBERS

Convert to improper fractions first

$$3\frac{1}{2} \times 2\frac{1}{3} = \frac{7}{2} \times \frac{7}{3} = \frac{49}{6} = 8\frac{1}{6}$$



Fraction button

Press SHIFT for the mixed number button

Mathematics – Angles & Polygons

What do I need to be able to do?

- Identify alternate angles
- Identify corresponding angles
- Identify co-interior angles
- Find the sum of interior angles in polygons
- Find the sum of exterior angles in polygons
- Find interior angles in regular polygon

Keywords:

- Parallel:** Straight lines that never meet
- Angle:** The figure formed by two straight lines meeting (measured in degrees)
- Transversal:** A line that cuts across two or more other (normally parallel) lines
- Isosceles:** Two equal size lines and equal size angles (in a triangle or trapezium)
- Polygon:** A 2D shape made with straight lines
- Sum:** Addition (total of all the interior angles added together)
- Regular polygon:** All the sides have equal length; all the interior angles have equal size.

Basic angle rules and notation

Acute Angles
 $0^\circ < \text{angle} < 90^\circ$

Right Angles
 90°

Obtuse
 $90^\circ < \text{angle} < 180^\circ$

Reflex
 $180^\circ < \text{angle} < 360^\circ$

Straight Line
 180°

Vertically opposite angles
 Equal
Angles around a point
 360°

The letter in the middle is the angle
 The arc represents the part of the angle

Angle Notation: three letters ABC
 This is the angle at B = 113°

Line Notation: two letters EG
 The line that joins E to G.

Parallel lines

Still remember to look for angles on straight lines, around a point and vertically opposite!

Lines OF and BE are transversals (lines that bsect the parallel lines)

Corresponding angles often identified by their "F shape" in position

Alternate angles often identified by their "Z shape" in position

This notation identifies parallel lines

Alternate/ Corresponding angles

Because alternate angles are equal the highlighted angles are the same size

Because corresponding angles are equal the highlighted angles are the same size

Co-interior angles

Because co-interior angles have a sum of 180° the highlighted angle is 110°

As angles on a line add up to 180° co-interior angles can also be calculated from applying alternate/ corresponding rules first

Properties of Quadrilaterals

Square
 All sides equal size
 All angles 90°
 Opposite sides are parallel

Rectangle
 All angles 90°
 Opposite sides are parallel

Rhombus
 All sides equal size
 Opposite angles are equal

Parallelogram
 Opposite sides are parallel
 Opposite angles are equal
 Co-interior angles

Trapezium
 One pair of parallel lines

Kite
 No parallel lines
 Equal lengths on top sides
 Equal lengths on bottom sides
 One pair of equal angles

Sum of interior angles

Interior Angles
 The angles enclosed by the polygon

Sum of the interior angles = $(n - 2) \times 180$

Sum of the interior angles = $(5 - 2) \times 180$

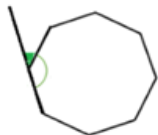
This shape can be made from three triangles
 Each triangle has 180°

Sum of the interior angles = $3 \times 180 = 540^\circ$

Remember this is all of the interior angles added together

This is an irregular polygon – the sides and angles are different sizes

Missing angles in regular polygons



$$\text{Exterior angle} = 360 \div 8 = 45^\circ$$

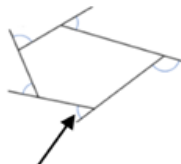
$$\text{Interior angle} = \frac{(8-2) \times 180}{8} = \frac{6 \times 180}{8} = 135^\circ$$

Exterior angles in regular polygons = $360^\circ \div$ number of sides

Interior angles in regular polygons = $\frac{(\text{number of sides} - 2) \times 180}{\text{number of sides}}$

Sum of exterior angles

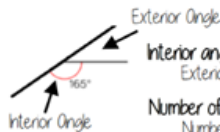
Exterior angles all add up to 360°



Exterior Angles

Are the angle formed from the straight-line extension at the side of the shape

Using exterior angles



Exterior Angle

$$\text{Interior angle} + \text{Exterior angle} = \text{straight line} = 180^\circ$$

$$\text{Exterior angle} = 180 - 165 = 15^\circ$$

$$\text{Number of sides} = 360^\circ \div \text{exterior angle}$$

$$\text{Number of sides} = 360 \div 15 = 24 \text{ sides}$$