## Mathematics – Developing number sense

# Reasoning with number



#### What do I need to be able to do?

#### By the end of this unit you should be able to:

- Know and use mental addition/subtraction
- Know and use mental multiplication/division
- Know and use mental arithmetic for decimals
- Know and use mental arithmetic for fractions
- Use factors to simplify calculations
- Use estimation to check mental calculations
- Use number facts
- Use algebraic facts

## Keywords

Commutative: changing the order of the operations does not change the result

I Ossociative: when you add or multiply you can do so regardless of how the numbers are grouped

Dividend: the number being divided
Divisor: the number we divide bu

Expression: a maths sentence with a minimum of two numbers and at least one math operation (no equals sign

**Equation**: a mathematical statement that two things are equal

Quotient: the result of a division

### Mental methods for addition/subtraction

<u>Oddition</u> is commutative

Subtraction the order has to stay the same



The order of addition does not change the result 360 - 147 = 360 - 100 - 40 - 7

Number lines help for addition

and subtraction

 Working in 10's first aids mental addition/ subtraction

## Mental methods for multiplication/division

Multiplication is commutative



2 × 4 = 4 × 2

The order of multiplication does not change the result Partitioning can help multiplication

24 x 6 = 20 x 6 + 4 x 6 = 120 + 24 = 144

Division is not associative

Chunking the division can help 4000 ÷ 25 "How many 25's in 100" then how many chunks of that in 4000.

### Mental methods for decimals

Multiplying by a decimal <1 will make the original value smaller - eg x 0.1 =  $\div$  10

Methods for multiplication 1,2 x 0.03

Methods for addition 23+24

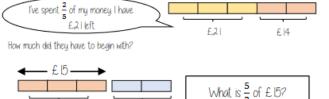
2 + 2 = 4 0.3 + 0.4 = 0.74 + 0.7 = 4.7 Methods for division  $15 \div 0.05$ 

Multiply by powers of 10 until the divisor becomes an integer

1.5 ÷ 0.05 ×100 × ×100 150 ÷ 5 = 30



Use bar models where possible



# Using factors to simplify calculations

30 x 16

10 x 3 x 4 x 4

2x5x3x2x2x2x2

10 x 3 x 2 x 8

16 x 10 x 3

Multiplication is commutative Factors can be multiplied in any order

## Estimation

Estimations are useful — especially when using fractions and decimals to check if your solution is possible.

Most estimations round to I significant figure

Estimations are useful — especially when using fractions and decimals to check if your solution is possible.

210 + 899 < 1200

This is true because even if both numbers were rounded up, they would reach 300 + 900

The correct estimation would be 200 + 900 - 1100.

## Number facts

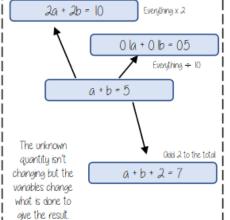
Use 124 x 5 = 620

For multiplication, each value that is multiplied or divided by powers of 10 needs to happen to the result

620÷ 124 = 50

For division you must consider the impact of the divisor becoming smaller or bigger. Smaller — the answer will be bigger (It is being shared into less parts) Bigger — the answer will be smaller (It is being shared into more parts)

## i <u>Olgebraic facts</u>



#### Mathematics – Prime Numbers & Proof

# Reasoning with number



#### What do I need to be able to do?

#### By the end of this unit you should be able to:

- Find and use multiples
- Identify factors of numbers and expressions
- Recognise and identify prime numbers
- Recognise square and triangular numbers
- Find common factors including HCF
- Find common multiples including LCM

## Keywords

Multiples: found by multiplying any number by positive integers

Factor: integers that multiply together to get another number.

Prime: an integer with only 2 factors.

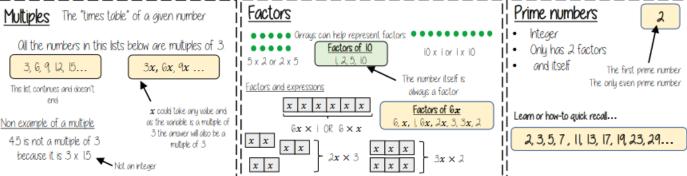
Conjecture: a statement that might be true (based on reasoning) but is not proven

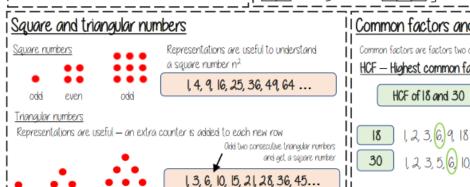
Counterexample: a special type of example that disproves a statement

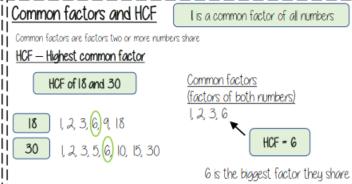
I | Expression: a maths sentence with a minimum of two numbers and at least one math operation (no equals sign)

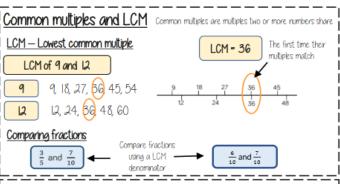
I HCF: highest common factor (biggest factor two or more numbers share)

I LCM: lowest common multiple (the first time the times table of two or more numbers match)









Counterexamples

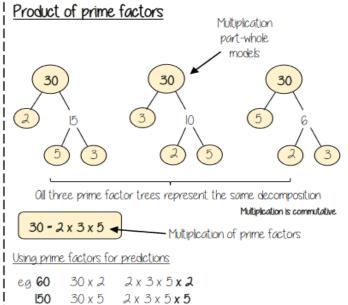
This sequence isn't doubling i

is adding 2 each time

Only one counterexample

is needed to disprove a

conjecture





Conjectures and counterexamples

<u>Conjecture</u>

1, 2, 4.... The numbers in the sequence are doubling each time.

a pattern that is

noticed for many

cases